

***Pedal axle calculations:***

***Input values:***

Axle diameter:  $d := 12 \cdot \text{mm}$   
Shank diameter:  $D := 18 \cdot \text{mm}$   
Original fillet radius:  $r := 2.0 \cdot \text{mm}$   
Compound fillet radius:  $r_2 := 6.0 \cdot \text{mm}$   
Compound fillet radius:  $r_1 := 1.4 \cdot \text{mm}$   
Diameter at line II:  $d_1 := 13.6 \cdot \text{mm}$   
ORIGIN  $\equiv 1$

***Calculation:***

Using Knovel Graph Digitizer for Chart 3.10:

Original condition:  $\frac{r}{d} = 0.167$

$$\frac{D}{d} = 1.5$$

Thus, the stress concentration factor is:  $K_t := 1.548$

At circumferential line I:  $\frac{r_2}{d} = 0.5$

$$\frac{D}{d} = 1.5$$

In this case, the stress concentration factor is  $K_{tI} := 1.322$

about:

$$\Delta\sigma := \frac{K_t - K_{tI}}{K_t}$$

**Stress reduction:**  $\Delta\sigma = 15\%$

At circumferential line II:  $\frac{r_1}{d_1} = 0.103$

$$\frac{D}{d_1} = 1.324$$

The stress concentration factor is:  $K_{tII} := 1.703$

Although the nominal diameter is larger at this section

Nominal stresses:  $\sigma_{\text{nomII}} = \frac{32 \cdot M}{\pi \cdot d_1^3}$

$$\sigma_{\text{nomI}} = \frac{32 \cdot M}{\pi \cdot d^3}$$

$$K_{\sigma} = \frac{\sigma_{\text{nomII}}}{\sigma_{\text{nomI}}}$$

Nominal stress reduction:  $K_{\sigma} := \frac{d^3}{d_1^3} \quad K_{\sigma} = 0.687$

Maximum stresses:  $\sigma_{\text{maxII}} = \sigma_{\text{nomII}} \cdot K_{tII} = \sigma_{\text{nom}} \cdot K_{tII} \cdot K_{\sigma}$

$$\sigma_{\text{maxI}} = \sigma_{\text{nom}} \cdot K_{tI}$$

$$\sigma_{\text{maxII}} = \sigma_{\text{maxI}} \cdot \frac{K_{tII} \cdot K_{\sigma}}{K_{tI}}$$

$$\sigma_{\text{rel}} = \frac{\sigma_{\text{maxII}}}{\sigma_{\text{maxI}}} = \frac{K_{tII} \cdot K_{\sigma}}{K_{tI}}$$

$$\sigma_{\text{rel}} := \frac{K_{tII} \cdot K_{\sigma}}{K_{tI}} \quad \sigma_{\text{rel}} = 0.885$$

the maximum stress  $\sigma_{\text{max2}}$  is smaller than  $\sigma_{\text{max1}}$ .

Consequently, stress reduction using double radius fillet is

$$\Delta\sigma = 15.0\%$$

**Using the equations to calculate stress concentration factors:**

$$\text{Shoulder height: } t := (D - d) \cdot 0.5 \quad t = 3 \cdot \text{mm}$$

$$\text{tr} := \frac{t}{r} \quad \text{tr} = 1.5$$

$$C := \begin{cases} \begin{pmatrix} 0.947 + 1.206 \cdot \sqrt{\text{tr}} - 0.13 \cdot \text{tr} \\ 0.022 - 3.405 \cdot \sqrt{\text{tr}} + 0.915 \cdot \text{tr} \\ 0.869 + 1.777 \cdot \sqrt{\text{tr}} - 0.555 \cdot \text{tr} \\ -0.810 + 0.422 \cdot \sqrt{\text{tr}} - 0.260 \cdot \text{tr} \end{pmatrix} & \text{if } \text{tr} \leq 2 \\ \begin{pmatrix} 1.232 + 0.832 \cdot \sqrt{\text{tr}} - 0.008 \cdot \text{tr} \\ -3.813 + 0.968 \cdot \sqrt{\text{tr}} - 0.260 \cdot \text{tr} \\ 7.423 - 4.868 \cdot \sqrt{\text{tr}} + 0.869 \cdot \text{tr} \\ -3.839 + 3.070 \cdot \sqrt{\text{tr}} - 0.600 \cdot \text{tr} \end{pmatrix} & \text{otherwise} \end{cases}$$

Stress concentration factor, original condition:

$$K_t := C_1 + C_2 \cdot \left(\frac{2 \cdot t}{D}\right) + C_3 \cdot \left(\frac{2 \cdot t}{D}\right)^2 + C_4 \cdot \left(\frac{2 \cdot t}{D}\right)^3$$

$$K_t = 1.524$$

At circumferential line I:

If filleting radius:  $r_2 = 6 \cdot \text{mm}$

$$\text{tr} := \frac{t}{r_2} \quad \text{tr} = 0.5$$

$$C := \begin{cases} \begin{pmatrix} 0.947 + 1.206 \cdot \sqrt{\text{tr}} - 0.13 \cdot \text{tr} \\ 0.022 - 3.405 \cdot \sqrt{\text{tr}} + 0.915 \cdot \text{tr} \\ 0.869 + 1.777 \cdot \sqrt{\text{tr}} - 0.555 \cdot \text{tr} \\ -0.810 + 0.422 \cdot \sqrt{\text{tr}} - 0.260 \cdot \text{tr} \end{pmatrix} & \text{if } \text{tr} \leq 2 \\ \begin{pmatrix} 1.232 + 0.832 \cdot \sqrt{\text{tr}} - 0.008 \cdot \text{tr} \\ -3.813 + 0.968 \cdot \sqrt{\text{tr}} - 0.260 \cdot \text{tr} \\ 7.423 - 4.868 \cdot \sqrt{\text{tr}} + 0.869 \cdot \text{tr} \\ -3.839 + 3.070 \cdot \sqrt{\text{tr}} - 0.600 \cdot \text{tr} \end{pmatrix} & \text{otherwise} \end{cases}$$

$$K_{tI} := C_1 + C_2 \cdot \left(\frac{2 \cdot t}{D}\right) + C_3 \cdot \left(\frac{2 \cdot t}{D}\right)^2 + C_4 \cdot \left(\frac{2 \cdot t}{D}\right)^3$$

$$K_{tI} = 1.274$$

$$\Delta\sigma := \frac{K_t - K_{tI}}{K_t}$$

**Stress reduction:**  $\Delta\sigma = 16\%$

At circumferential line II:

$$\text{Partial shoulder height: } t := (D - d_1) \cdot 0.5 \quad t = 2.2 \cdot \text{mm}$$

$$\text{tr} := \frac{t}{r_1} \quad \text{tr} = 1.571$$

$$C := \begin{cases} \begin{pmatrix} 0.947 + 1.206 \cdot \sqrt{\text{tr}} - 0.13 \cdot \text{tr} \\ 0.022 - 3.405 \cdot \sqrt{\text{tr}} + 0.915 \cdot \text{tr} \\ 0.869 + 1.777 \cdot \sqrt{\text{tr}} - 0.555 \cdot \text{tr} \\ -0.810 + 0.422 \cdot \sqrt{\text{tr}} - 0.260 \cdot \text{tr} \end{pmatrix} & \text{if } \text{tr} \leq 2 \\ \begin{pmatrix} 1.232 + 0.832 \cdot \sqrt{\text{tr}} - 0.008 \cdot \text{tr} \\ -3.813 + 0.968 \cdot \sqrt{\text{tr}} - 0.260 \cdot \text{tr} \\ 7.423 - 4.868 \cdot \sqrt{\text{tr}} + 0.869 \cdot \text{tr} \\ -3.839 + 3.070 \cdot \sqrt{\text{tr}} - 0.600 \cdot \text{tr} \end{pmatrix} & \text{otherwise} \end{cases}$$

Stress concentration factor:

$$K_{tII} := C_1 + C_2 \cdot \left(\frac{2 \cdot t}{D}\right) + C_3 \cdot \left(\frac{2 \cdot t}{D}\right)^2 + C_4 \cdot \left(\frac{2 \cdot t}{D}\right)^3$$

$$K_{tII} = 1.691$$

$$\sigma_{\text{rel}} := \frac{K_{tII} \cdot K_{\sigma}}{K_{tI}} \quad \sigma_{\text{rel}} = 0.912$$

the maximum stress  $\sigma_{\text{max}2}$  is smaller than  $\sigma_{\text{max}1}$ .

Consequently, stress reduction using double radius fillet is

$$\Delta\sigma = 16\%$$